

# STAT 213 Model Selection II

Colin Reimer Dawson

Oberlin College

March 30, 2018

1 / 13

Notes

---



---



---



---



---



---



---

## Outline

Model Selection

Exploring Model Space

2 / 13

Notes

---



---



---



---



---



---



---

## Outline

Model Selection

Exploring Model Space

3 / 13

Notes

---



---



---



---



---



---



---

## So many models...

- How to decide among all these models?
  1. Understand the subject area! Build sensible models.
  2. Nested  $F$ -tests
  3. Model quality measures

4 / 13

Notes

---

---

---

---

---

---

---

---

## What Makes a Good Model?

### Fit

---

High  $R^2$   
Small  $SSE$   
Large  $F$

### Validity

---

Strong evidence for predictors  
Simple (Parsimonious)  
Generalizes outside sample

5 / 13

Notes

---

---

---

---

---

---

---

---

## Why Does Parsimony Matter?

Don't we just care about good predictions?

Not exclusively...

- We also use models to *understand* the world (harder with more complexity)

And even so...

- We really care about making predictions for data we *haven't seen yet*.

6 / 13

Notes

---

---

---

---

---

---

---

---

## Criteria to “score” models

1. high  $R^2$ /low SSE/low  $\hat{\sigma}_\epsilon^2$ : always prefers more complex models
2. Adj.  $R^2$ : balances fit and complexity
3. Mallows's  $C_p$  / Akaike Information Criterion (AIC): estimates mean squared prediction error based on  $\hat{\sigma}_\epsilon^2$  from a “full” model
4. Out-of-sample predictive accuracy (next time)

7 / 13

Notes

---

---

---

---

---

---

---

---

## Mallows's $C_p$ / AIC

Two measures that reduce to the same thing in the case of MLR with independent, equal variance, Normal residuals. For a “reduced” model with  $p_{\text{reduced}}$  total parameters (including the intercept) which is nested in a “full” model with  $p_{\text{full}}$  parameters, both fit using  $n$  observations:

$$C_p = \frac{SSE_{\text{reduced}}}{MSE_{\text{full}}} + 2p_{\text{reduced}} - n \quad (1)$$

$$= p_{\text{reduced}} + \frac{SSE_{\text{diff}}}{MSE_{\text{full}}} \quad (2)$$

where smaller values indicate a simpler model (smaller  $p_{\text{reduced}}$ ) and/or a better fit (smaller  $SSE_{\text{diff}}$ )

8 / 13

Notes

---

---

---

---

---

---

---

---

## Outline

Model Selection

Exploring Model Space

9 / 13

Notes

---

---

---

---

---

---

---

---

## Model Selection

Five predictor-selection methods:

1. Domain knowledge (+ a few  $F$ -tests)
2. Best subset
3. Forward selection
4. Backward selection
5. Stepwise selection

10 / 13

Notes

---

---

---

---

---

---

---

---

## Automated exploration of predictor subsets

1. Best subset: consider all possible combinations ( $2^K$ )
2. Forward selection: start with null model, and consider adding one predictor at a time
3. Backward elimination: start with full model and consider removing one predictor at a time
4. Stepwise regression: consider both additions and subtractions at each iteration

Note: Choose best step based on adj- $R^2$  or  $C_p$ /AIC, *not* based on  $P$ -values

11 / 13

Notes

---

---

---

---

---

---

---

---

## Model Selection

		"Scoring"		
		$R^2_{adj.}$	$C_p$	CV Error (next time)
"Search"	Domain Knowledge			
	Best Subset			
	Forward Selection			
	Backward Selection			
	Stepwise Selection			

12 / 13

Notes

---

---

---

---

---

---

---

---

# Example: Baseball Win %

Demo

13 / 13

Notes

---

---

---

---

---

---

---

---

Notes

---

---

---

---

---

---

---

---

Notes

---

---

---

---

---

---

---

---